

# Axino dark matter and baryon asymmetry from Q-ball decay in gauge mediation

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Ref.: SK, Kawakami, Kawasaki, arXiv:1202.4067

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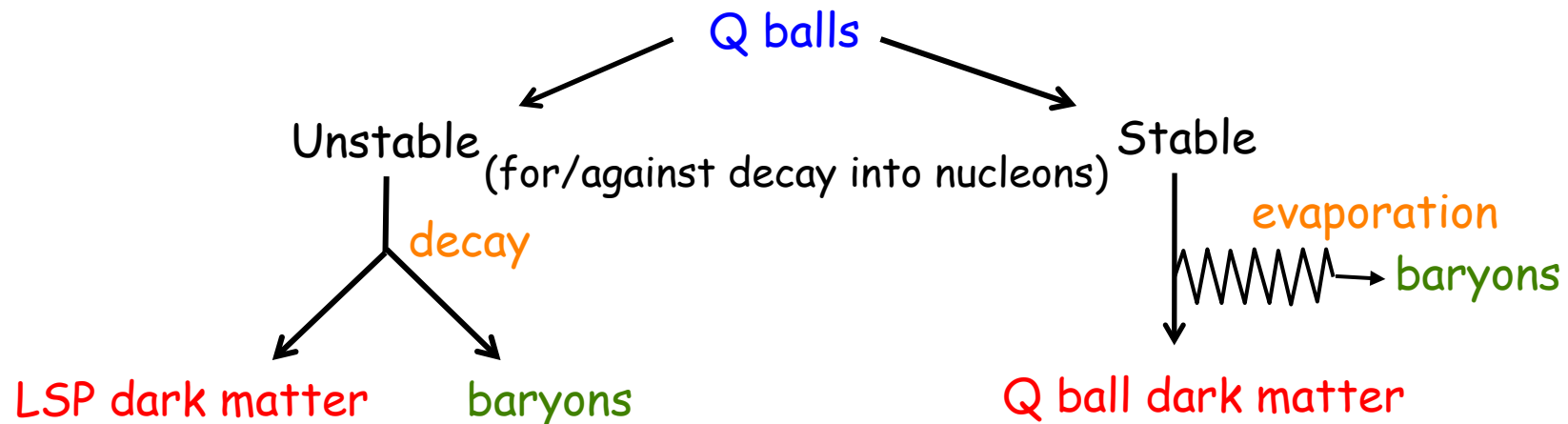
# 1. Introduction

## Affleck-Dine & Q-ball cosmology

Simultaneous explanation for the **dark matter** & **baryon asymmetry** in the universe.

- The Affleck-Dine (AD) mechanism is very promising for baryogenesis.
- The AD field consists of some combinations of squarks in MSSM.
- The AD condensate transforms into **Q balls**.

**Q balls** will provide both the **dark matter** and **baryon asymmetry**.

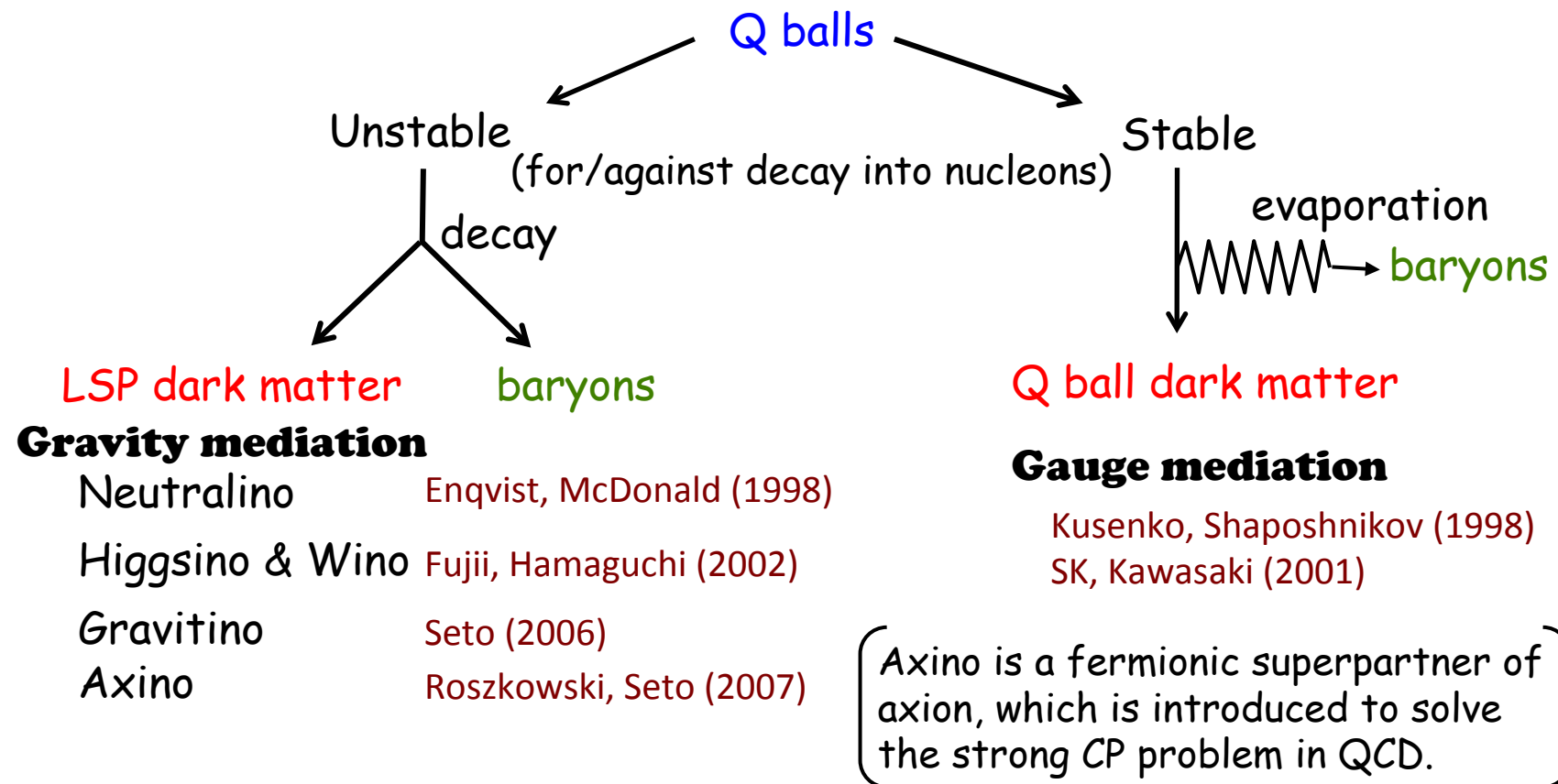


Abundances have a direct relation because of the same origin.

# 1. Introduction

Affleck-Dine & Q-ball cosmology

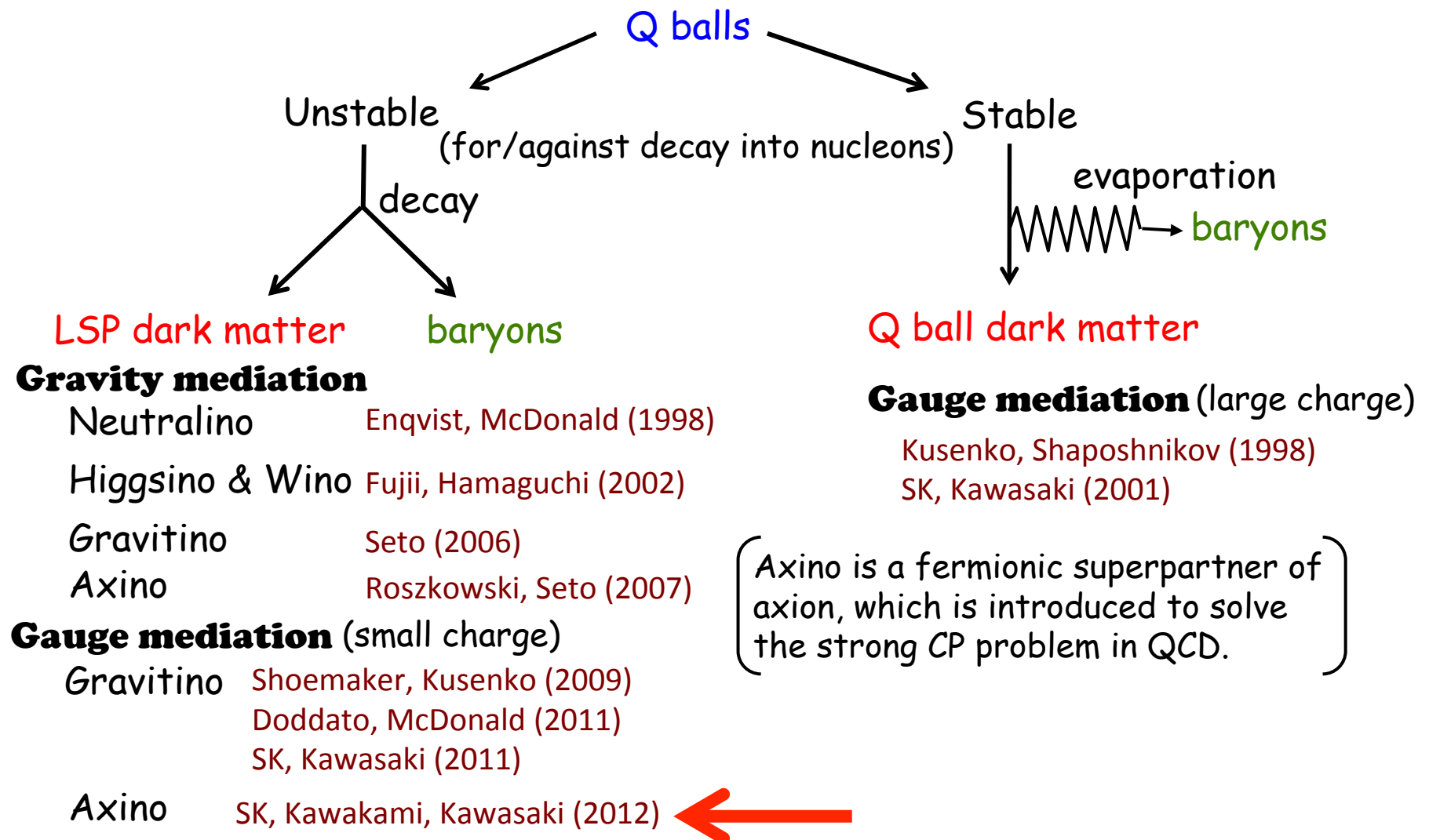
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# 1. Introduction

Affleck-Dine & Q-ball cosmology

Q balls will provide both the **dark matter** and **baryon asymmetry**.



# What to be shown

Very simple scenario to explain  
both **DM** and **B** in gauge mediation.

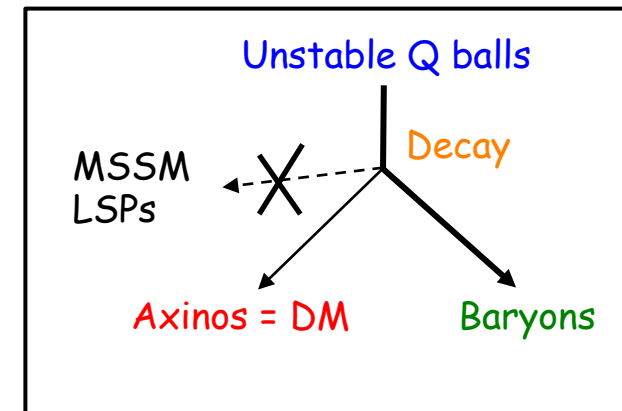
Affleck-Dine condensate  $\longrightarrow$  Q balls

If the Q-ball charge is **small enough to decay into nucleons**,  
but **large enough to be kinematically**  
**forbidden to decay into MSSM LSPs**,

$\Rightarrow$  Q balls are unstable and decay  
mainly into nucleons,  $\longrightarrow$  **Baryons**  
partially into axinos,  $\longrightarrow$  **DM**  
hardly into MSSM LSPs.  $\longrightarrow$  Not spoiling BBN

The rate of the decay **into nucleons is saturated**,  
**into axino is generally small, but could be saturated**.

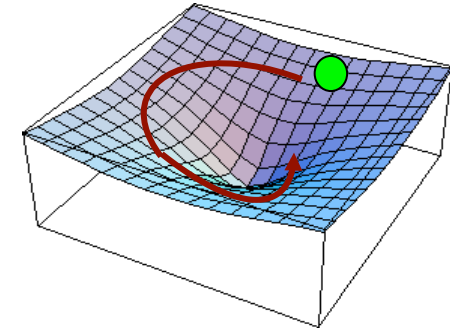
With oblate orbit of AD field  $\longrightarrow \Omega_b \sim 0.2 \Omega_{DM}$



## 2. Affleck-Dine baryogenesis

### Affleck-Dine mechanism

Affleck, Dine (1985)



(1) Affleck-Dine (AD) field has large VEV during inflation.

(2) Starts rotation when  $H \sim m_{\text{eff}} (= \sqrt{V''})$ , after inflation.

$\Rightarrow$  Baryon number production  $Q = \int d^3x \phi^2 \dot{\theta} \quad \left( \Phi = \frac{1}{\sqrt{2}} \phi e^{i\theta} \right)$

(3) AD field decays into quarks.

### MSSM flat direction works as AD field.

Affleck, Dine (1985), Dine, Randall, Thomas (1996)

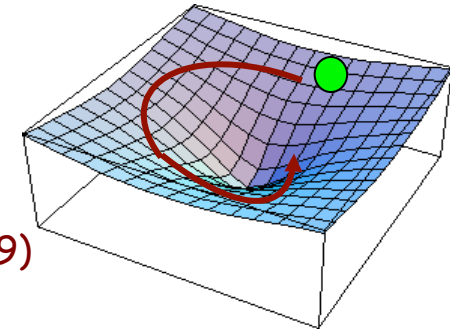
The MSSM flat direction is a scalar field consists of squarks, sleptons and maybe higgs whose potential vanishes along that direction.

$$\left( \begin{array}{ll} \text{Some examples:} & \\ \text{LH}_u & \text{dddLL} \\ \text{udd} & \text{uuuee} \\ \text{LLe} & \text{QuQue} \\ \text{QdL} & \end{array} \right)$$

## 2a. Affleck-Dine **Q-ball** baryogenesis

### Affleck-Dine Q-ball mechanism

Kusenko, Shaposhnikov (1998), Enqvist, McDonald (1998,1999)  
SK, Kawasaki (2000,2001)



(1) Affleck-Dine (AD) field has large VEV during inflation.

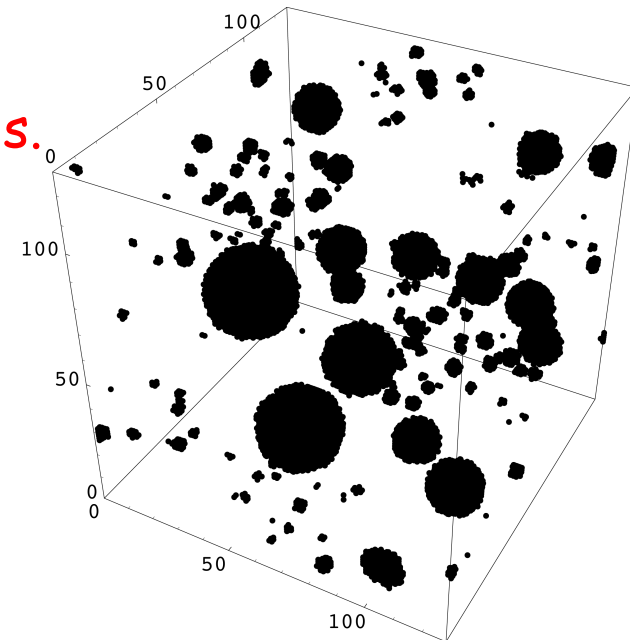
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~~(3) AD field decays into quarks.~~

(3) AD condensate disintegrates into Q balls.

(4) Q balls emits baryons.  
(through the decay or  
the evaporation in thermal bath)

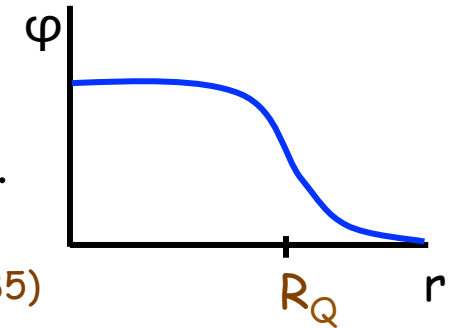


SK, Kawasaki (2001)

### 3. Q ball in gauge mediation

A Q ball is a kind of **non-topological soliton**, the energy min. configuration of the scalar field with **non-zero charge Q**.

Coleman (1985)



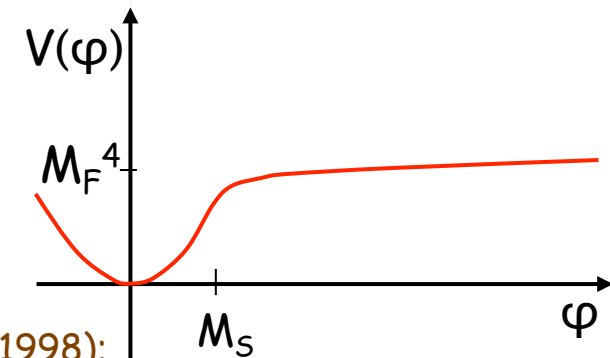
The potential of the AD field is lifted by SUSY breaking effects, and in the gauge mediation it reads as

$$V(\Phi) = \begin{cases} m_\phi^2 |\Phi|^2, & (|\Phi| \ll M_S) \\ M_F^4 \left( \log \frac{|\Phi|^2}{M_S^2} \right)^2, & (|\Phi| \gg M_S) \end{cases}$$

$$m_\phi \sim O(\text{TeV})$$

$$10^3 \text{ GeV} \lesssim M_F \lesssim \frac{g^{1/2}}{4\pi} \sqrt{m_{3/2} M_P}$$

Kusenko, Shaposhnikov (1998);  
de Gouvêa, Moroi, Murayama (1997)



Q balls form during the helical motion of the AD condensate.

$$Q = \beta \left( \frac{\phi_{\text{osc}}}{M_F} \right)^4$$

$$\beta = \begin{cases} 6 \times 10^{-4} & (\varepsilon = 1) \\ 6 \times 10^{-5} & (\varepsilon \lesssim 0.1) \end{cases}$$

SK, Kawasaki (2001)

$$\text{Baryon \#}: B = bQ$$

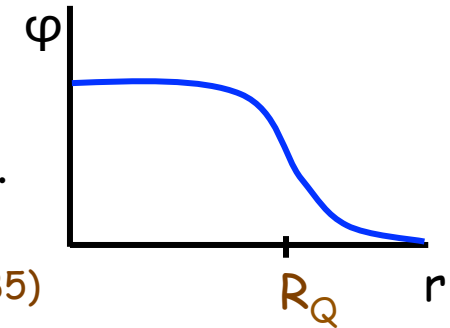
$$\begin{cases} M_Q \simeq \frac{4\sqrt{2}\pi}{3} M_F Q^{3/4}, \\ R_Q \simeq \frac{1}{\sqrt{2}} M_F^{-1} Q^{1/4}, \\ \omega_Q \simeq \sqrt{2}\pi M_F Q^{-1/4}, \\ \phi_Q \simeq M_F Q^{1/4}, \end{cases}$$



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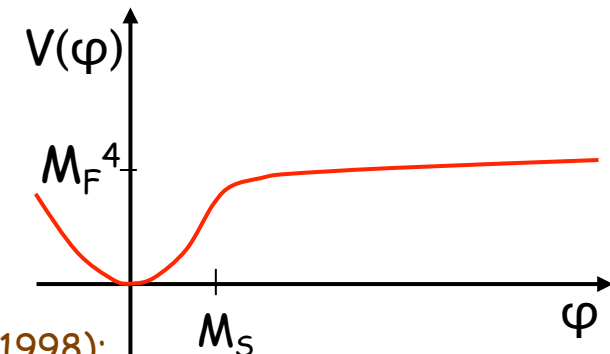
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## 4. Q-ball Decay

### Kinematics

The Q ball can decay if the mass per charge  $M_Q/Q$  ( $\sim Q^{-1/4}$ ) is larger than the decay-particle mass  $m_D$ .

$$m_D < \frac{M_Q}{Q} \left( \propto Q^{-1/4} \right) \implies Q < \frac{1024\pi^4}{81} \left( \frac{M_F}{m_D} \right)^4$$

#### **Allowed**

(i) Decay into nucleons ( $m_N \approx 1 \text{ GeV}$ , i.e.,  $m_D \approx 0.3 \text{ GeV}$  for  $b=1/3$ )

(ii) Decay into axinos ( $m_{\tilde{a}} < \text{GeV}$ ) ( $m_{\tilde{a}} = m_{3/2}$  is assumed)

#### **Forbidden**

(iii) Decay into MSSM LSPs ( $m_{\text{MLSP}} = O(100) \text{ GeV}$ )

$$\implies Q_{\text{cr}} \equiv 10^{11} \left( \frac{M_D}{100 \text{ GeV}} \right)^{-4} < Q < 10^{21} \left( \frac{M_D/b}{\text{GeV}} \right)^{-4} \quad (\text{for } M_F = 10^4 \text{ GeV})$$

Only after the charge becomes smaller than  $Q_{\text{cr}}$ , MSSM LSPs would be produced.

SK, Takahashi (2007); SK, Kawasaki (2011)

# 4. Q-ball Decay

## Decay rates

The decay process takes place on the surface, and the rate is given by

Cohen, Coleman, Georgi, Manohar (1986)

$$\Gamma_Q \simeq \begin{cases} \Gamma_Q^{(\text{sat})} & (f_{\text{eff}} \phi_Q \gtrsim \omega_Q) \\ 3\pi \frac{f_{\text{eff}} \phi_Q}{\omega_Q} \Gamma_Q^{(\text{sat})} & (f_{\text{eff}} \phi_Q \ll \omega_Q) \end{cases} \quad \Gamma_Q^{(\text{sat})} \simeq \frac{1}{Q} \frac{\omega_Q^3}{192\pi^2} 4\pi R_Q^2 \simeq \frac{\pi^2}{24\sqrt{2}} M_F Q^{-5/4}$$

$$\mathcal{L}_{\text{int}} = f_{\text{eff}} \phi \psi \bar{\psi}$$

(i) Decay into nucleons **saturated**

$$\Gamma_Q = \Gamma_Q^{(\text{sat})} \implies T_D \simeq 4.3 \text{ MeV} \left( \frac{M_F}{10^4 \text{ GeV}} \right)^{1/2} \left( \frac{Q}{10^{21}} \right)^{-5/8}$$

Decay before BBN

(ii) Decay into axinos **saturated/unsaturated**

$$B_{\tilde{a}} \equiv \frac{\Gamma_Q^{(\tilde{a})}}{\Gamma_Q^{(\text{sat})}} \simeq 4.8 \times 10^{-4} \left( \frac{f_a}{10^{14} \text{ GeV}} \right)^{-1} \log \left( \frac{f_a}{10^3 \text{ GeV}} \right) \left( \frac{Q}{10^{21}} \right)^{\frac{1}{2}} \quad f_{\text{eff}}^{(\tilde{a})} = \frac{\alpha_s^2}{\sqrt{2}\pi^2} \frac{m_{\tilde{g}}}{f_a} \log \left( \frac{f_a}{m_{\tilde{g}}} \right)$$

Covi et al. (2002)

For saturated case,  $B_{\tilde{\alpha}} = 1$ .

(iii) Decay into gravitinos **unsaturated**

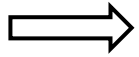
$$B_{3/2} \equiv \frac{\Gamma_Q^{(3/2)}}{\Gamma_Q^{(\text{sat})}} \simeq \sqrt{3}\pi^2 \frac{M_F^2}{m_{3/2} M_P} \lesssim 0.1 g_s \ll 1 \quad f_{\text{eff}}^{(3/2)} \simeq \frac{1}{\sqrt{6}} \frac{\omega_Q^2}{m_{3/2} M_P}$$

Gravitino production is negligible.

## 5. Abundances

Since AD field rotates with ellipticity  $\varepsilon$ , the Q ball decays into **nucleons**, partially into **axinos** with branching ratio  $B_{\tilde{a}}$ , and into **MSSM LSPs** only with fraction  $Q_{\text{cr}}/Q$ , the number densities are related to  $\Phi$ -numbers as

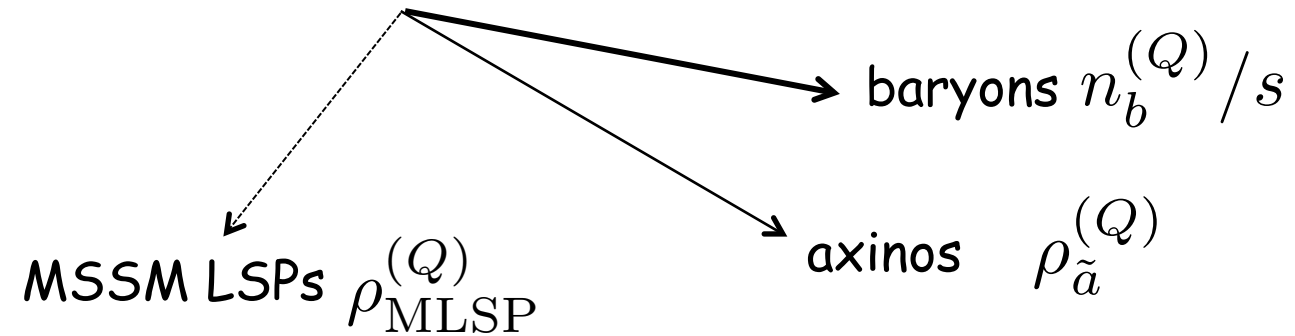
$$\begin{aligned}
 n_b &\simeq \varepsilon b n_\phi \\
 n_{\tilde{a}} &\simeq B_{\tilde{a}} n_\phi \\
 n_{\text{MLSP}} &\simeq \frac{Q_{\text{cr}}}{Q} n_\phi
 \end{aligned}
 \quad + \quad
 \begin{aligned}
 Y_b &\simeq \frac{3}{4} T_{\text{RH}} \left. \frac{n_b}{\rho_{\text{inf}}} \right|_{\text{osc}} \\
 \rho_{\tilde{a}} / \rho_b &\simeq 5 \\
 \frac{\rho_{\text{MLSP}}}{s} &\simeq 5 m_N Y_b \frac{\rho_{\text{MLSP}}}{\rho_{\tilde{a}}}
 \end{aligned}$$



$$\left\{ \begin{aligned}
 \left. \frac{Y_b}{10^{-10}} \right|_{\text{sat}} &\simeq 2.3 \times 10^2 \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right) \left( \frac{\beta}{6 \times 10^{-5}} \right)^{-3/4} \left( \frac{T_{\text{RH}}}{10^7 \text{ GeV}} \right) \left( \frac{M_F}{10^4 \text{ GeV}} \right) \left( \frac{Q}{10^{21}} \right)^{3/4} \\
 \left. \frac{Y_b}{10^{-10}} \right|_{\text{unsat}} &\simeq 0.11 \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right) \left( \frac{f_a}{10^{14} \text{ GeV}} \right)^{-1} \log \left( \frac{f_a}{10^3 \text{ GeV}} \right) \left( \frac{\beta}{6 \times 10^{-5}} \right)^{-3/4} \left( \frac{T_{\text{RH}}}{10^7 \text{ GeV}} \right) \left( \frac{M_F}{10^4 \text{ GeV}} \right) \left( \frac{Q}{10^{21}} \right) \\
 \left. \frac{\rho_{\text{MLSP}}}{s} \right|_{\text{sat}} &\simeq 6.2 \times 10^{-18} \text{ GeV} \left( \frac{Y_b}{10^{-10}} \right) \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right)^{-1} \left( \frac{m_{\text{MLSP}}}{100 \text{ GeV}} \right)^{-3} \left( \frac{M_F}{10^4 \text{ GeV}} \right)^4 \left( \frac{Q}{10^{21}} \right)^{-1}, \\
 \left. \frac{\rho_{\text{MLSP}}}{s} \right|_{\text{unsat}} &\simeq 1.3 \times 10^{-14} \text{ GeV} \left( \frac{Y_b}{10^{-10}} \right) \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right)^{-1} \left( \frac{f_a}{10^{14} \text{ GeV}} \right) \left( \log \frac{f_a}{10^3 \text{ GeV}} \right)^{-1} \left( \frac{m_{\text{MLSP}}}{100 \text{ GeV}} \right)^{-3} \left( \frac{M_F}{10^4 \text{ GeV}} \right)^4 \left( \frac{Q}{10^{21}} \right)^{-3/2}
 \end{aligned} \right.$$

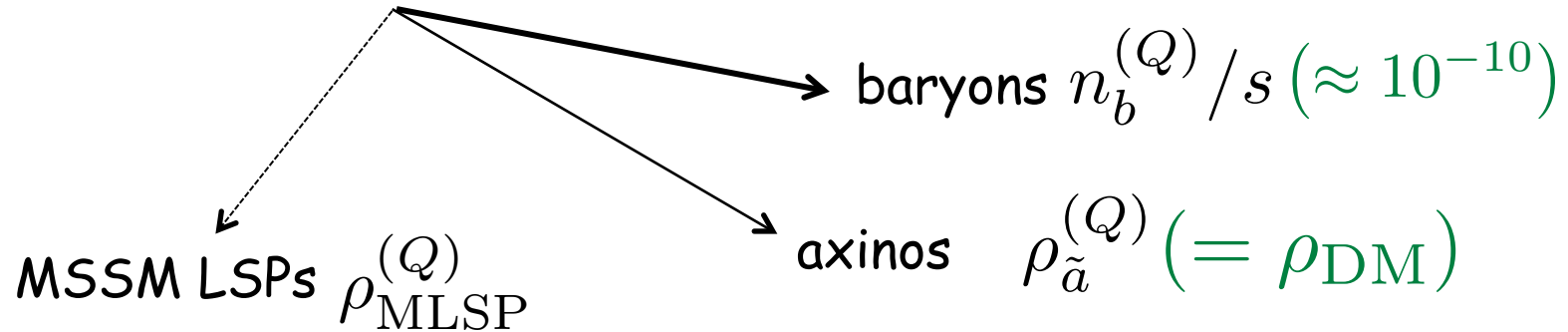
## 6. Constraints on abundances

Q-ball decay at  $T=T_D$



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Q-ball decay at  $T=T_D$  ( $> 3\text{MeV}$ )



MSSM LSP abundance has an upper limit in order not to spoil the BBN.

$$\rho_{\text{MLSP}}^{(Q)} < \rho_{\text{MLSP}}^{(\text{BBN})}$$

Thermally produced gravitinos/axinos do not contribute to DM density.

$$\rho_{3/2}^{(\text{TH})}, \rho_{\tilde{a}}^{(\text{TH})} < \rho_{\tilde{a}}^{(Q)}$$

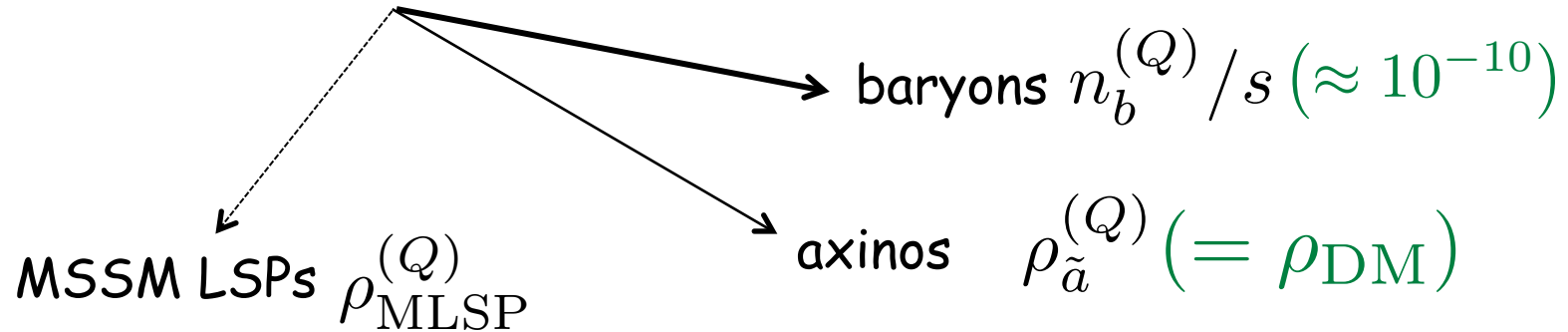
⇒ Highest possible  $T_{\text{RH}}$

$$\left[ \begin{array}{l} \text{gravitino } T_{\text{RH,max}}^{(3/2)} = 3 \times 10^7 \text{ GeV} \left( \frac{m_{3/2}}{\text{GeV}} \right) \quad \text{Moroi, Murayama, Yamaguchi (1993)} \\ \quad \text{Kawasaki, Takahashi, Yanagida (2006)} \\ \\ \text{axino } \Omega_{\text{KSVZ } \tilde{a}}^{\text{TH}} h^2 \simeq 10^{-2} \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right) \left( \frac{f_a}{10^{14} \text{ GeV}} \right)^{-2} \left( \frac{T_{\text{RH}}}{10^7 \text{ GeV}} \right) \longrightarrow T_{\text{RH,max}}^{(\text{KSVZ } \tilde{a})} = 10^8 \text{ GeV} \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right)^{-1} \left( \frac{f_a}{10^{14} \text{ GeV}} \right)^2 \\ \Omega_{\text{DFSZ } \tilde{a}}^{\text{TH}} h^2 \simeq \begin{cases} 10^{-3} \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right) \left( \frac{f_a}{10^{14} \text{ GeV}} \right)^{-2} \left( \frac{T_{\text{RH}}}{10^7 \text{ GeV}} \right) & (T_{\text{RH}} \gtrsim 2 \times 10^7 \text{ GeV}) \\ 2 \times 10^{-3} \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right) \left( \frac{f_a}{10^{14} \text{ GeV}} \right)^{-2} & (T_{\text{RH}} \lesssim 2 \times 10^7 \text{ GeV}) \end{cases} \longrightarrow T_{\text{RH,max}}^{(\text{DFSZ } \tilde{a})} = 10^9 \text{ GeV} \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right)^{-1} \left( \frac{f_a}{10^{14} \text{ GeV}} \right)^2 \\ \hspace{15em} \longrightarrow \left( \frac{m_{\tilde{a}}}{\text{GeV}} \right) \left( \frac{f_a}{10^{14} \text{ GeV}} \right)^{-2} \lesssim 55 \\ \hspace{15em} T_{\text{RH,max}}^{(3/2)} \text{ is imposed.} \end{array} \right]$$

Covi et al. (2001), Brandenburg, Steffen (2004), Strumia (2010), Chun (2011), Choi et al. (2012), SK, Kawakami, Kawasaki (2012)

# 6. Constraints on abundances

Q-ball decay at  $T=T_D$  ( $> 3\text{MeV}$ )



MSSM LSP abundance has an upper limit in order not to spoil the BBN.

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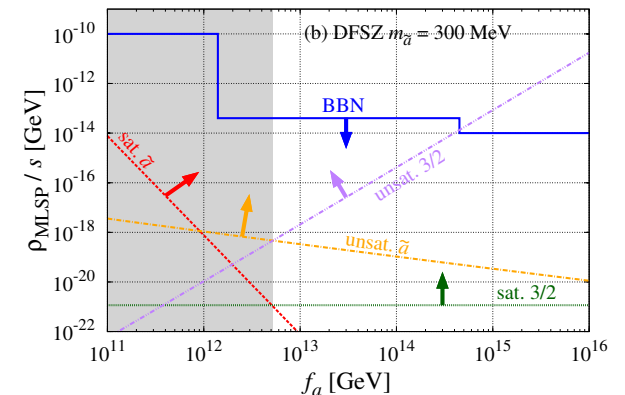
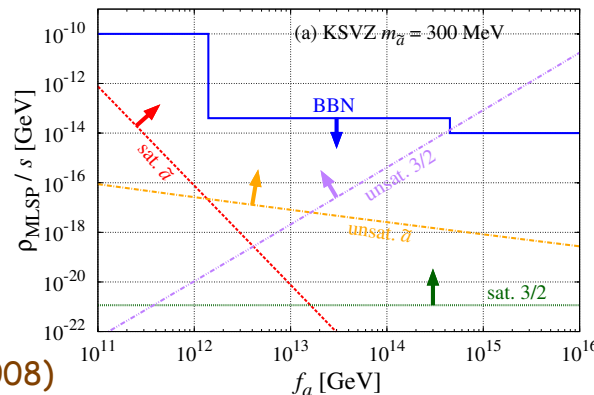
$$\rho_{3/2}^{(\text{TH})}, \rho_{\tilde{a}}^{(\text{TH})} < \rho_{\tilde{a}}^{(Q)}$$

⇒ Highest possible  $T_{\text{RH}}$

Lowest possible MLSP abundance  $\rho_{\text{MLSP},\text{min}}^{(Q)}$

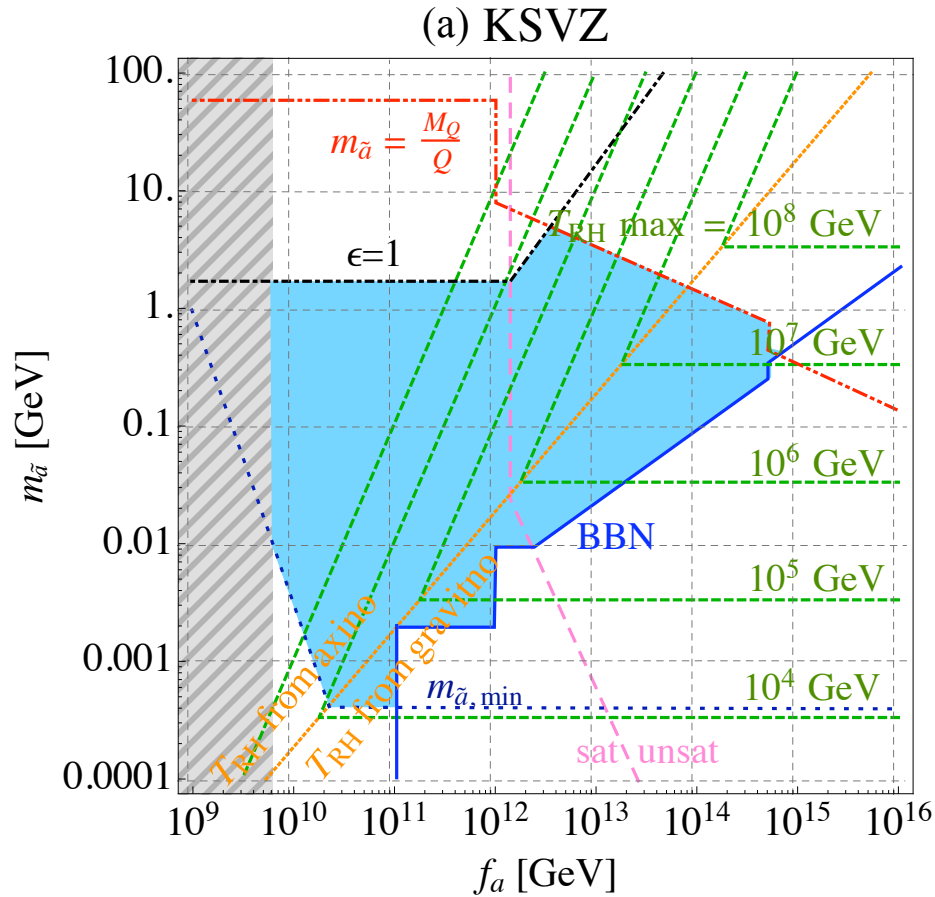
$$\rho_{\text{MLSP},\text{min}}^{(Q)} < \rho_{\text{MLSP}}^{(\text{BBN})}$$

BBN constraints from  
 Kawasaki, Kohri, Moroi (2005)  
 Kohri, Moroi, Yotsuyanagi (2006)  
 Kawasaki, Kohri, Moroi, Yotsuyanagi (2008)

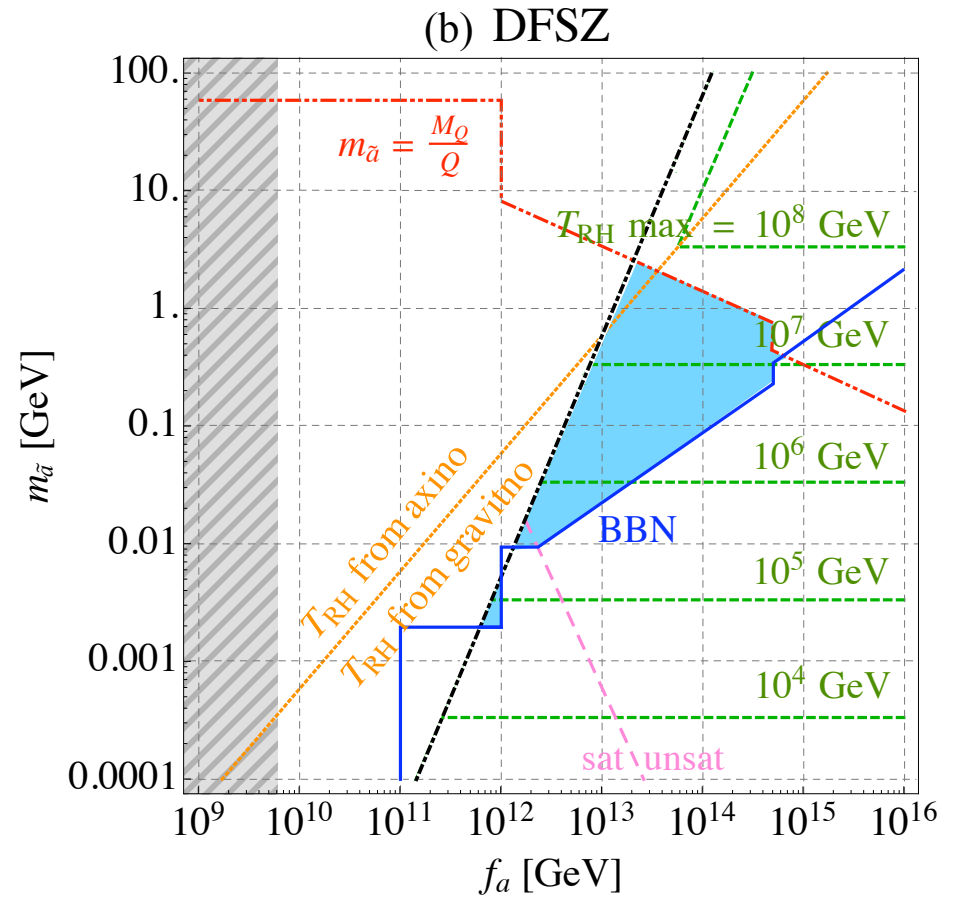


# 7. Allowed regions

Axino parameter space ( $f_a, m_{\tilde{a}}$ )



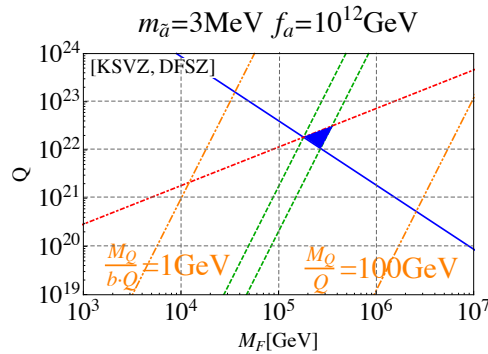
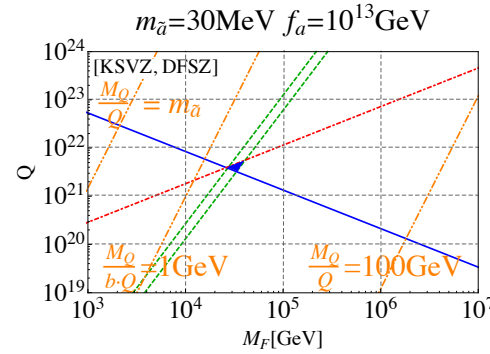
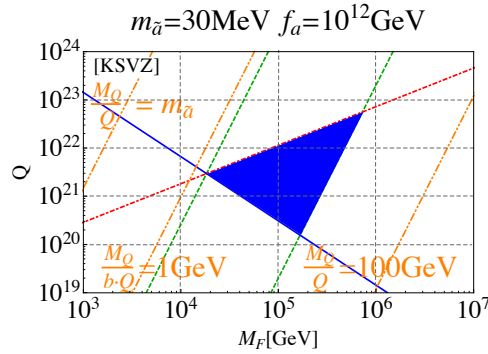
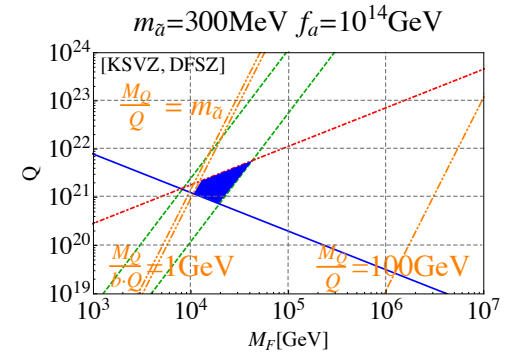
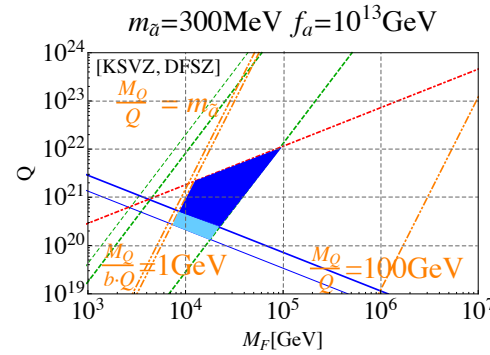
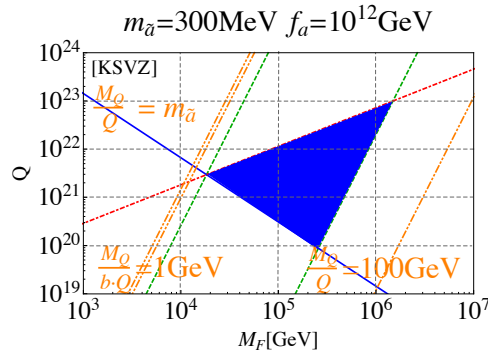
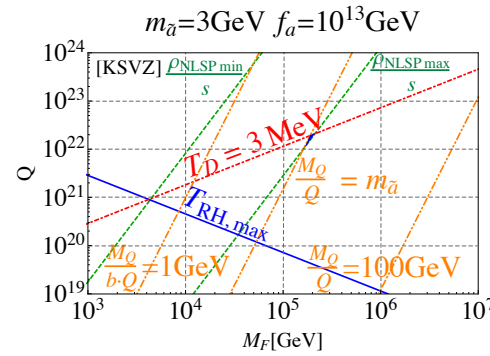
$6 \times 10^9 \text{ GeV} < f_a < 5 \times 10^{14} \text{ GeV}$   
 $m_{\tilde{a}} = O(\text{MeV}) - O(\text{GeV})$



$10^{12} \text{ GeV} < f_a < 5 \times 10^{14} \text{ GeV}$   
 $m_{\tilde{a}} = O(10 \text{ MeV}) - O(\text{GeV})$



# Q-ball parameter space ( $M_F$ , $Q$ )

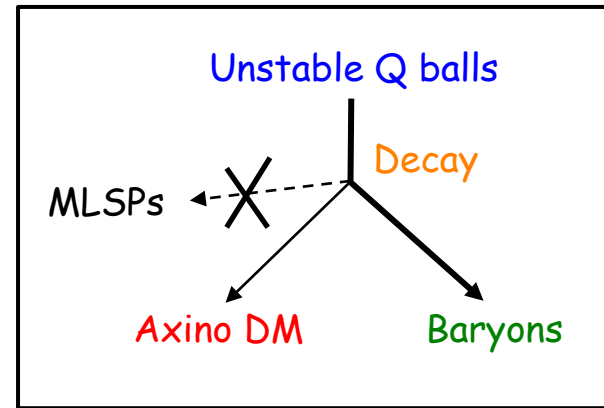


$$Q = 10^{20} - 10^{22}$$

$$M_F = 10^4 - 10^6 \text{ GeV}$$

## 8. Conclusions

Very simple scenario to explain  
both DM and B in GMSB.



Unstable Q balls decay mainly into nucleons,  $\rightarrow$  Baryons  
partially into axinos,  $\rightarrow$  DM  
hardly into MSSM LSPs.  $\rightarrow$  Not spoiling BBN  
(Still, small amount created constrains the model.)

The Q-ball charge is small enough to decay into nucleons,  
large enough not to decay into MSSM LSPs.  
 $\rightarrow T_D \sim O(10 \text{ MeV})$

The rate of the decay into nucleons is saturated,  
into axinos is not saturated  
(saturated in some cases).

$\Omega_b \sim 0.2 \Omega_{DM}$  can be explained.