Hidden Sector Assisted 125 GeV Higgs

Bumseok KYAE  
(Pusan Nat’l Univ.)

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in collaboration with Jong-Chul Park (KIAS)

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@ PLANCK
ATLAS, CMS reported the excesses of events for $\gamma\gamma$, $ZZ^*$, $WW^* \rightarrow 4$ leptons around 125 GeV.

They seemingly imply the presence of the Higgs with 125 GeV mass at 3$\sigma$ level.
Higgs mass in the MSSM

- At tree level

$$m_h^2 < M_Z^2 \cos^2 2\beta$$

- LEP bound: $$m_h^2 > 114 \text{ GeV}$$.

- By including the radiative corrections, the Higgs mass can be raised above 100 GeV.
Radiative Corr. to $m_h^2$ in the MSSM

$$\Delta m_h^2 = \left(\frac{3}{4\pi^2}\right) (y_tM_t)^2 \sin^2\beta \log\left( M_t^2+m_t^2/M_t^2\right)$$

($y_t$: top quark Yukawa coupling, $M_t$: top quark mass, $m_t$: S-top mass)

For a large radiative correction to the Higgs mass, the S-top should be quite heavy.

(a few TeV for $m_h=125$ GeV)
Radiative Corr. to $m_h^2$
in the MSSM

The other piece of $\Delta V_{cw}$” contributes to the renormalization of $m_{2h}^2$.

One of the extremum conditions with the MSSM Higgs pot. reads

$$m_{2h}^2 = m_{12}^2 \cot \beta + (M_Z^2/2)\cos2\beta$$
$$- (3y_t^2/8\pi^2) \left[ m_t^2 \{ \log(m_t^2/\Lambda^2)-1 \} - M_t^2 \{ \log(M_t^2/\Lambda^2)-1 \} \right]$$

A large $m_t$ (a few TeV) requires a fine-tuning (0.1%) among the soft parameters to fit $M_Z$.

“Little Hierarchy Problem”
Large mixing between the L- and R-hnd. S-tops through the “A-term” is helpful for raising $m_h$:

$$\Delta m_h^2 \approx \left(\frac{3}{4\pi^2}\right) (y_t M_t)^2 \sin^2 \beta \left[ \log \left( \frac{m_t^2}{M_t^2} \right) + \left( \frac{X_t}{m_t} \right)^2 \left\{ 1 - \left( \frac{X_t}{m_t} \right)^2 / 12 \right\} \right]$$

$$X_t = A_t - \mu \cot \beta$$

The maximal mixing $[ (X_t/m_t)^2 = 6 ]$ can push $m_h$ up to 135 GeV. But, ...
Higgs mass in the NMSSM

- promote the MSSM $\mu$ term to $\lambda S H_u H_d$ in the superpot., introducing a singlet $S$.
- The Higgs mass can be raised to

$$m_h^2 \approx M_Z^2 \cos^2 2\beta + \lambda^2 v_H^2 \sin^2 2\beta + \Delta m_h^2$$

- But $\lambda$ is restricted by the Landau pole constraint:

$$\lambda < 0.7$$

- For $m_t = O(100)$ GeV, $0.5 < \lambda < 0.7$, $1 < \tan \beta < 3$. 
By introducing extra order one Yukawa coupling of extra unknown matter, 125 GeV Higgs mass can be explained without a serious fine-tuning.

But introduction of new colored particles with order one Yukawa couplings would exceedingly affect 1. the production rate of \( gg \rightarrow h \) and also 2. the decay rate of \( h \rightarrow \gamma\gamma \) at the LHC.

\[ \rightarrow \text{immoderate deviation from the SM prediction} \]
Can the Radiative Correction be enhanced by MSSM singlets?
1-loop Effective Potential in the MSSM

\[ y_t H_u Q_3 t^c \]

+ bosonic loops

+ ...
1-loop Effective Potential by SM Singlets

\[ \left( \frac{y_{HN}}{M_*} \right) H_u H_d N N^c + M_N N N^c \]

+ bosonic loops
1-loop Effective Potential by SM Singlets

\[ \langle H_u \rangle \rightarrow S^c \rightarrow \langle H_d \rangle \]
1-loop Effective Potential by SM Singlets

\[ \langle H_u \rangle \quad \langle H_d \rangle \]

\[ S^c \]

\[ N \quad N^c \]

\[ M_N^* \]
1-loop Effective Potential by SM Singlets

\[ W_{\text{eff}} = \mu H_u H_d + y_H S H_u H_d + M_S S S^c + y_N S^c N N^c + M_N N N^c \]
A singlet extension of the MSSM

Introducing neutral fields under SM, \( \{S, S^c\}, \{N, N^c\} \), where \( \{N, N^c\} \) are n-dim. Rep. of a (large) Hidden gauge group.

\[
W = y_H S H_u H_d + M_S S S^c + y_N S^c N N^c + M_N N N^c
\]

\[ + W_{\text{MSSM}} \text{ (}\mu\text{ term included)} \]

\( y_H < O(1), \ y_N \sim O(1) \)

\( y_N \) does NOT blow up at higher energies.
A singlet extension of the MSSM

Introducing neutral fields under SM, \{S, S^c\}, \{N, N^c\},
where \{N, N^c\} are n-dim. Rep. of a (large) Hidden gauge group.

Visible sec. \hspace{1cm} Messenger sec. \hspace{1cm} Hidden sec.

\[
W = y_H S H_u H_d + M_S S S^c + y_N S^c N N^c + M_N N N^c + W_{MSSM} \text{ (}\mu\text{ term included)}
\]

\(y_H \sim O(1), \ y_N \sim O(1) \quad M_S, M_N < 1 \text{ TeV} \), e.g. by G.-M. mech.
A singlet extension of the MSSM

At the min. of the potential,

\[ \langle S \rangle \approx (\text{soft para.}) \times \langle H_u H_d \rangle \]

\[ \langle S^c \rangle \approx - \left( \frac{y_H}{M_S} \right) \langle H_u H_d \rangle \]

SUSY mass\(^2\) of \(\{N,N^c\} = [M_N - \left( \frac{y_H y_N}{M_S} \right) \langle H_u H_d \rangle]^2\]

\[ \approx M_N - 2 \left( \frac{y_H y_N M_N}{M_S} \right) \langle H_u H_d \rangle \]

→ insert it in the C.-W. pot.
Radiative Corr. to $m_{h}^{2}$ by the Singlets

$$\Delta m_{h}^{2} = \left(\frac{n}{4\pi^{2}}\right) (y_{N}M_{N}/M_{S})^{2} (y_{H}^{2}v_{H}^{2}\sin^{2}2\beta) \log\left(\frac{M_{N}^{2}+m_{N}^{2}}{M_{N}^{2}}\right)$$

$\Delta m_{h}^{2}$ can be enlarged by $n$, $(y_{N}M_{N}/M_{S})^{2}$, etc.

Compared with the case of the MSSM:

$$\Delta m_{h}^{2} |_{\text{top}} = \left(\frac{3}{4\pi^{2}}\right) (y_{t}M_{t})^{2} \sin^{2}\beta \log\left(\frac{M_{t}^{2}+m_{t}^{2}}{M_{t}^{2}}\right)$$

($y_{t}$: top quark Yukawa coupling, $M_{t}$: top quark mass, $m_{t}$: S-top mass)
Radiative Corr. to $m_h^2$ by the Singlets

$$\Delta m_h^2 = \left(\frac{n}{4\pi^2}\right)(y_N M_N/M_S)^2(y_H v_H^2 \sin^2 2\beta) \log\left(M_N^2 + m_N^2/M_N^2\right)$$

Note:

- Above $M_S$, $\Delta V(H)$ can NOT be a local op. any longer.
- $y_N (\sim O(1))$ does NOT blow up at higher energies.
Radiative Corr. to $m_{h^2}$ by the Singlets

The other piece of $\Delta V''$ contributes to the renormalization of $m_{12}^2$.

One of the extremum conditions becomes

$$-2m_{12}^2 = (m_{1h}^2 - m_{2h}^2) \tan 2\beta + M_Z^2 \sin 2\beta$$

$$-\left( 4\pi^2 \right) \left( y_N M_N / M_S \right) \left[ m_N^2 \log \left( m_N^2 / \Lambda^2 \right) - 1 \right] - M_N^2 \log \left( M_N^2 / \Lambda^2 \right) - 1$$
Radiative Corr. to $m_h^2$ by the Singlets

$$\Delta m_h^2 = (n/4\pi^2) \left( y_N M_N / M_S \right)^2 \left( y_H^2 v_H^2 \sin^2 2\beta \right) \log \left( M_N^2 + m_N^2 / M_N^2 \right)$$

$$-2m_{12}^2 = (m_{1h}^2 - m_{2h}^2) \tan 2\beta + M_Z^2 \sin 2\beta$$

$$-\left( n y_H / 4\pi^2 \right) \left( y_N M_N / M_S \right) \left[ m_N^2 \left\{ \log (m_N^2 / \Lambda^2) - 1 \right\} - M_N^2 \left\{ \log (M_N^2 / \Lambda^2) - 1 \right\} \right]$$

Compared with the MSSM/4\textsuperscript{th} family scenario,

$$\Delta m_h^2 = (3/4\pi^2) \left( y_t M_t \right)^2 \sin^2 \beta \ \log \left( M_t^2 + m_t^2 / M_t^2 \right)$$

$$m_{2h}^2 = m_{12}^2 \cot \beta + (M_Z^2 / 2) \cos 2\beta$$

$$-\left( 3y_t^2 / 8\pi^2 \right) \left[ m_t^2 \left\{ \log (m_t^2 / \Lambda^2) - 1 \right\} - M_t^2 \left\{ \log (M_t^2 / \Lambda^2) - 1 \right\} \right]$$
FIG. 2: Contour plots for the lightest Higgs mass $m_h$ in the $y_H - m_N$ plane. Here we set $\Delta m_h^{2\text{top}} = (66 \text{ GeV})^2$, which corresponds to $\tilde{m}_t \approx 500 \text{ GeV}$ at two-loop level, but turn off the mixing effect. The tree level contribution from the NMSSM is ignored. We fix the other parameters as shown in the figure. The thick dashed line corresponds to $m_h = 125 \text{ GeV}$. 
FIG. 3: Lightest Higgs mass $m_h = 125$ GeV lines for various $\tan\beta$s in the $y_H - m_S$ plane. Here we set $\Delta m_h|_{\text{top}}^2 = (66 \text{ GeV})^2$, which corresponds to $\tilde{m}_t \approx 500$ GeV at two-loop level, but turn off the mixing effect. The tree level contribution from the NMSSM is ignored. The other parameters are fixed as shown in the figure.
The Model

\[ W_{UV} = y_H S H_u H_d + y_N \overline{S N \overline{N}} + \frac{f_1}{M_P} \Sigma_1^2 H_u H_d + \frac{f_2}{M_P} \Sigma_2^2 N \overline{N} + \frac{f_3}{M_P} \Sigma_3^2 S \overline{S} + \frac{g_1}{M_P} \Sigma_3 \Sigma_1 \overline{\Sigma_1} + \frac{g_2}{M_P} \Sigma_3 \Sigma_2 \overline{\Sigma_2} + \frac{g_3}{M_P} \Sigma_3^2 \overline{\Sigma_3} \]
The Model

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TABLE I. R and Pecci-Quinn charges of the superfields. The MSSM *matter* superfields carry the unit $R$ charges, and also the PQ charges of 1/8. $N$ and $\overline{N}$ are assumed to be proper $n$-dimensional vector-like representations of a hidden gauge group, under which all the MSSM fields are neutral. $\Sigma$s and $\overline{\Sigma}$s carry some $Z_2$ charges.
The “A-terms” corresponding to the $g_1, g_2, g_3$ terms and the soft mass terms admit the VEVs,

$$< \Sigma_{1,2,3} > \sim < \Sigma^c_{1,2,3} > \sim (m_{3/2}M_P)^{1/2}$$

Then,

$$f_i \Sigma_i^2 / M_P \sim m_{3/2}.$$ So $\mu, M_S, M_N$ are of EW scale.
The “A-terms” corresponding to the $g_1, g_2, g_3$ terms and the soft mass terms admit the VEVs,

$$\langle \Sigma_{1,2,3} \rangle \sim \langle \Sigma^c_{1,2,3} \rangle \sim (m_{3/2}M_P)^{1/2}$$

The domain wall problem can be avoided, if $T_r < 10^9$ GeV.
• **SUSY Higgs mass** can increase through the radiative correction by 1 TeV scale Hidden sector fields, which can communicate with the Higgs via the messenger fields with 300 – 500 GeV masses.

• Even for $0.2 < y_H < 0.5$ or $3 < \tan\beta < 10$, 125 GeV Higgs mass can be naturally explained with relatively light S-top mass ($\approx 500$ GeV) but without their mixing effect.

• **No serious fine-tuning** because the mass para. for 125 GeV Higgs are all just around a few hundred GeV to 1 TeV.