

What Next for Cosmology ?

On the experimental front:

CMB polarization

Non-gaussianity

Baryon acoustic oscillations

Sunyaev-Zeldovich detection of clusters

Weak and strong lensing

Supernovae surveys

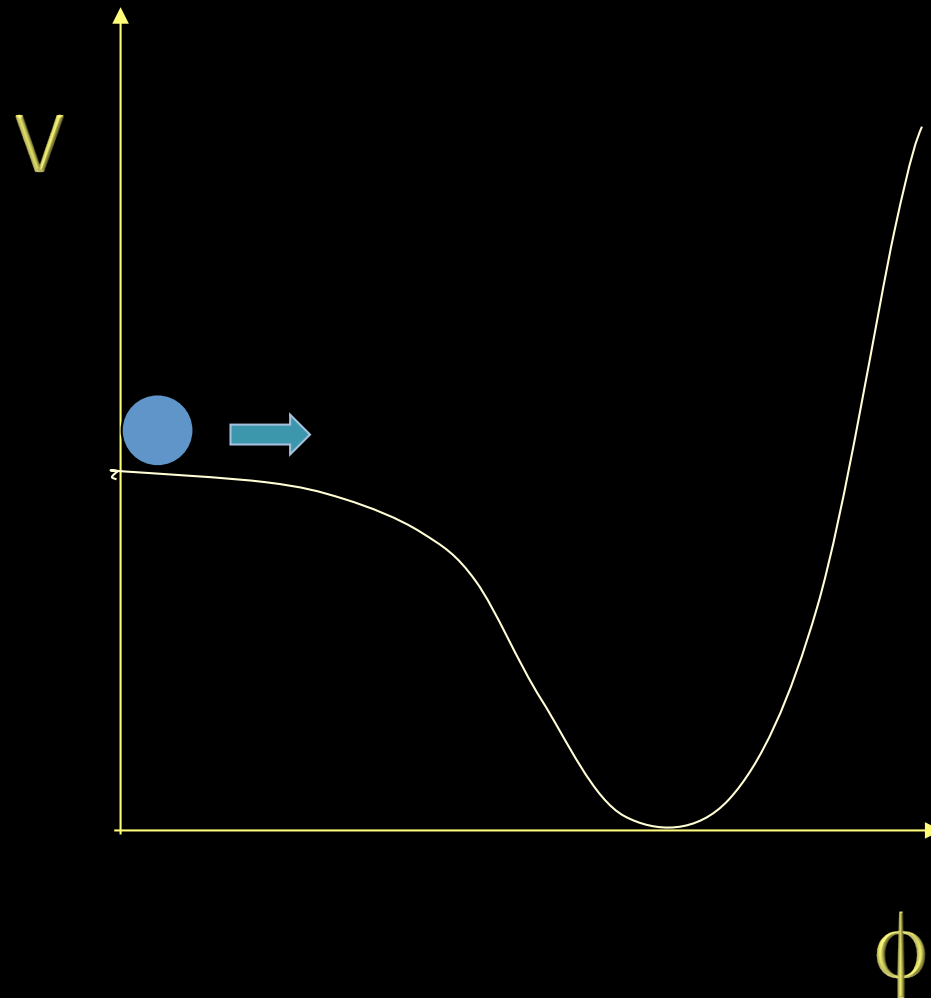
Dark matter searches

Direct g-wave detection

On the theoretical front:

CRISIS

Big bang inflationary picture



Explanatory & Predictive Power

Inflation explains homogeneity and flatness beginning from
arbitrary initial conditions

Inflation is powerfully predictive

flat

nearly scale-invariant perturbations

slightly red tilt

adiabatic

gaussian

gravitational waves

consistency relations

Guth
Hawking
Bardeen, PJS, Turner
Mukhanov & Chibisov
Starobinskii

....

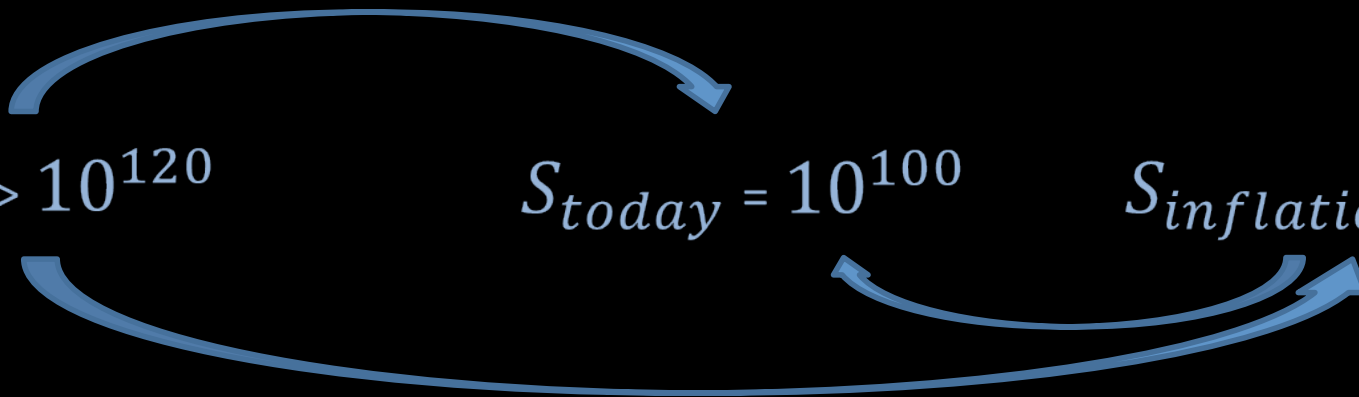
Inflation explains homogeneity and flatness beginning from
arbitrary initial conditions



$$S_{max} > 10^{120}$$

$$S_{today} = 10^{100}$$

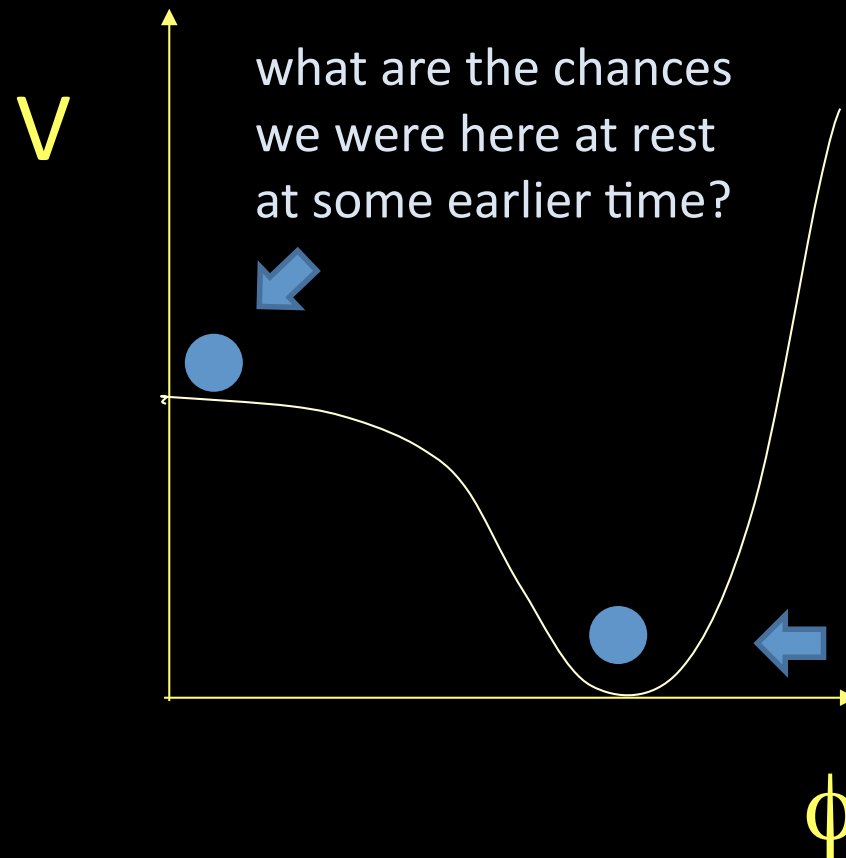
$$S_{inflation} < 10^{20}$$



$$\# \text{ states} \sim \text{likelihood} \sim e^S$$

$$KE \sim 1/a^6 \text{ as } a \rightarrow 0$$

$$PE \rightarrow \text{constant}$$



inflaton field

“LIOUVILLE PROBLEM”

For precise evaluation, see
Gibbons & Turok (2006)
Turok (2012)

if we start from conditions at the
end of smoothing &
extrapolate backwards ...

Why was this not appreciated before? Were we duped?

Chaotic inflating universe

A. D. Linde

P. N. Lebedev Physics Institute, Academy of Sciences of the USSR

(Submitted 31 May 1983)

Pis'ma Zh. Eksp. Teor. Fiz. **38**, No. 3, 149–151 (10 August 1983)

It is shown that **inflation is a natural result of chaotic initial conditions** in the early universe. These initial conditions are found in a wide class of elementary particle theories.

to point, and it is only later that the universe became uniform and isotropic.⁵ Let us assume that the magnitude of the classical field ϕ at first also had different random values at different points in space, and let us follow the evolution of the field ϕ in time. We are interested in the regions of space where the field ϕ , for accidental reasons, was quite uniform. If the size of the corresponding region at first exceeded the size of the

Explanatory & Predictive Power

Inflation explains homogeneity and flatness beginning from
arbitrary initial conditions



Inflation is overly predictive



at
nearly scale-invariant perturbations
slightly red tilt
adiabatic
gaussian
gravitational waves
consistency relations

“the classic(al) perspective”

dominantly a classical process...

an ordering process...

in which quantum physics plays
a small but important perturbative role

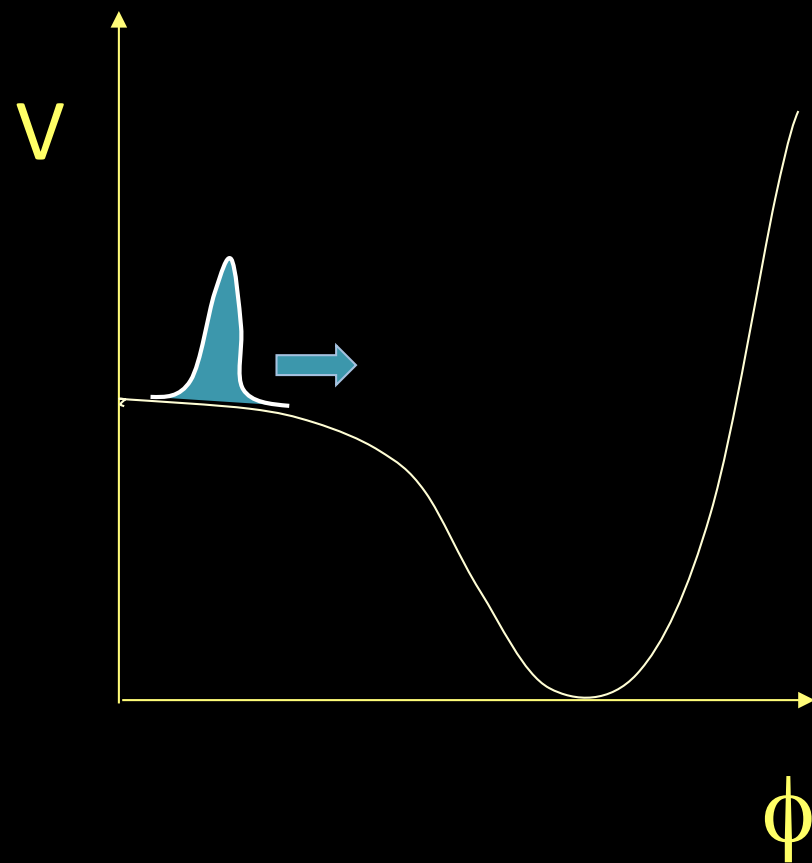
“the (true) quantum perspective”

Inflation is dominantly a quantum process...

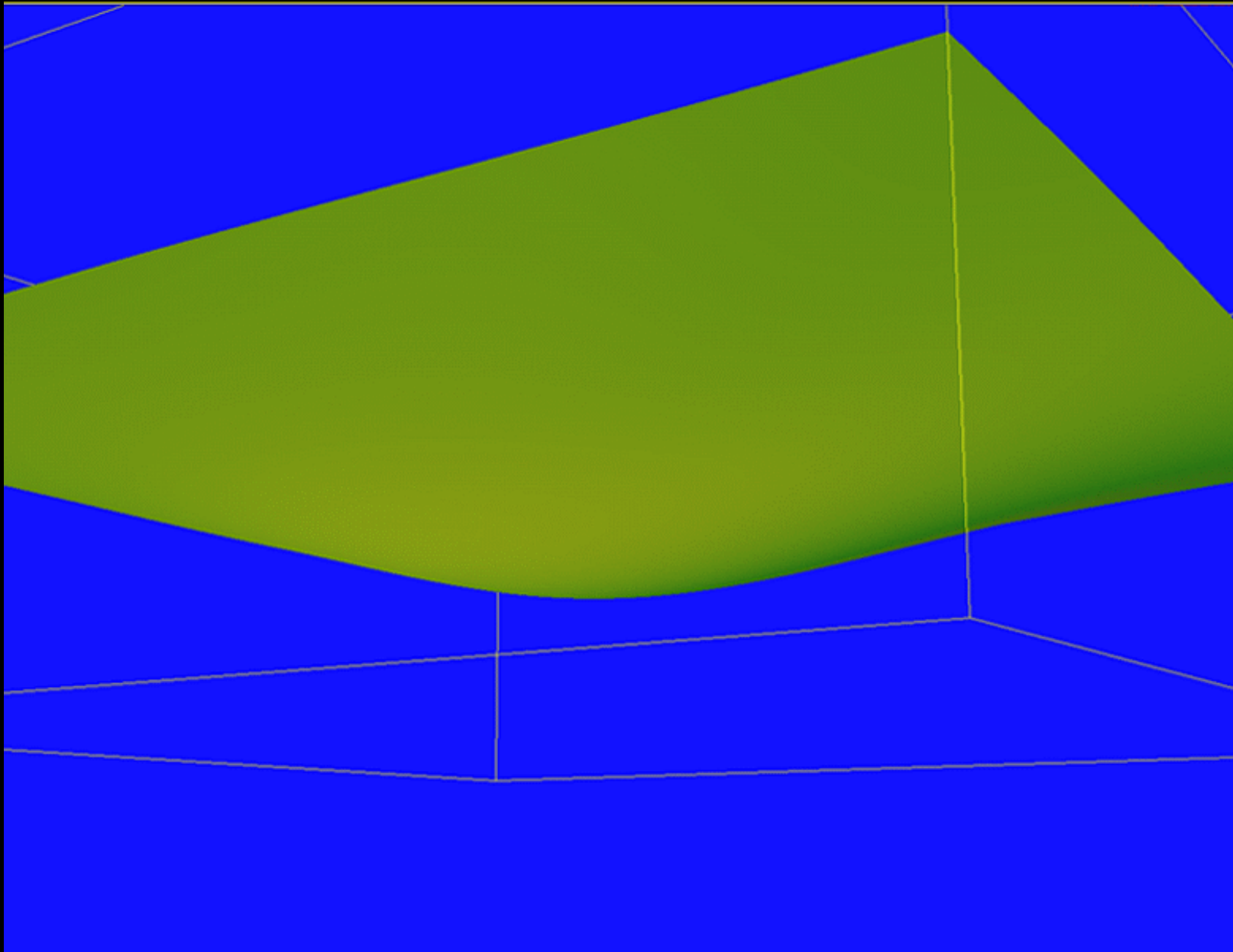
in which (classical) inflation amplifies
rare quantum fluctuations...

resulting in a peculiar kind of disorder

Eternal Inflation




Vilenkin, 1983
PJS, 1983



Linde, Linde, Mezhlumian, PRD 50, 2456 (1994)

Linde, Linde, Mezhlumian, PRD 50, 2456 (1994)



Anything that can happen will happen
--- and it will happen an infinite number of times

Eternal inflation is not an option – it is a feature:

A consequence of the fact that you want the
inflationary expansion rate
to exceed the decay rate of the inflationary phase

Predictability Problem



The Great Leap Backwards



volume measures
(Boltzmann brain & youngess problem)

proper time measures
(youngness problem)

causal patch measures
(predictions depends on initial conditions)

scale factor measures
(many versions, our universe not preferred)

anthropic principle

Maybe we should be satisfied
that at least some regions can be
like what we observe ?

Noooooooooo !!!!!

Time to Rethink Cosmology

Inflation is the only way of solving
the causal horizon problem

Inflation is the only way
of “flattening” the universe

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Inflation is the only way
of “flattening” the universe

$$H^2 = \frac{8\pi G}{3} \left(\frac{\rho_m^0}{a^3} + \frac{\rho_r^0}{a^4} + \dots \right) - \frac{k}{a^2}$$

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$$H^2 = \frac{8\pi G}{3} \left(\frac{\rho_m^0}{a^3} + \frac{\rho_r^0}{a^4} + \dots \right) - \frac{k}{a^2} + \frac{8\pi G}{3} \rho_{\text{inflaton}}$$

Time to Rethink Cosmology

Inflation is the only way of solving
the causal horizon problem

Inflation is the only way
of “flattening” the universe

Inflation is the only way
of generating scale invariant perturbations

ultra-slow contraction with $w \gg 1$:

$$H^2 = \frac{8\pi G}{3} \frac{\rho_m^0}{a^3} + \frac{8\pi G}{3} \frac{\rho_r^0}{a^4} + \frac{\sigma^2}{a^6} + \dots - \frac{k}{a^2}$$

$$+ \frac{8\pi G}{3} \frac{\rho_\phi^0}{a^{3(1+w)}} \leftarrow w \gg 1$$

$$a(t) \sim t^{2/3(1+w)} \equiv t^{1/\varepsilon}$$

ultra-slow contraction with $w \gg 1$:

quantum fluct. exit horizon & re-enter later

$$\varepsilon \equiv \frac{3}{2}(1 + w)$$

$$\text{wavelength} \sim a(t) \sim t^{\frac{1}{\varepsilon}} \sim (H^{-1})^{\frac{1}{\varepsilon}} \sim (\text{Horizon})^{1/\varepsilon}$$

rapid expansion

***wavelength grows
much faster than horizon***

$$\varepsilon \ll 1 \text{ (or } w \sim -1)$$

slow contraction

***wavelength shrinks
much slower than horizon***

$$\varepsilon \gg 1 \text{ (or } w \gg 1)$$

ultra-slow contraction with $w \gg 1$:

Tensor fluctuations are completely different

Amplitude $\sim H^2$

rapid expansion

slow contraction

H large

H exponentially small

H nearly constant

H increasing

$r \sim 25\%$

$r \sim$ exponentially small

same argument applies to axions

In sum, with a bounce & no inflation:

Can causally smooth

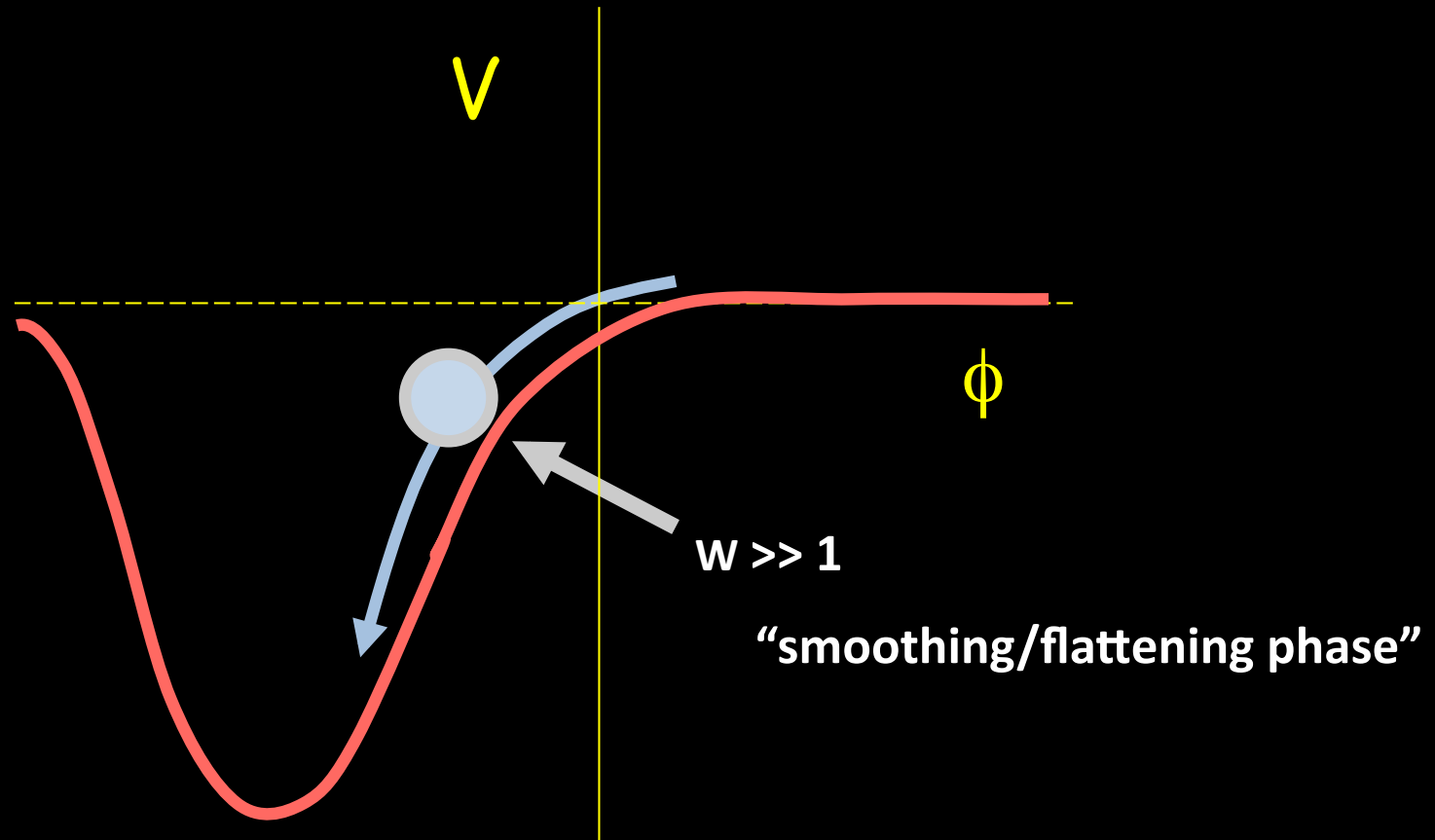
Can flatten

Can isotropize

Can make density perturbations

But is that all ?

$w > 1$?

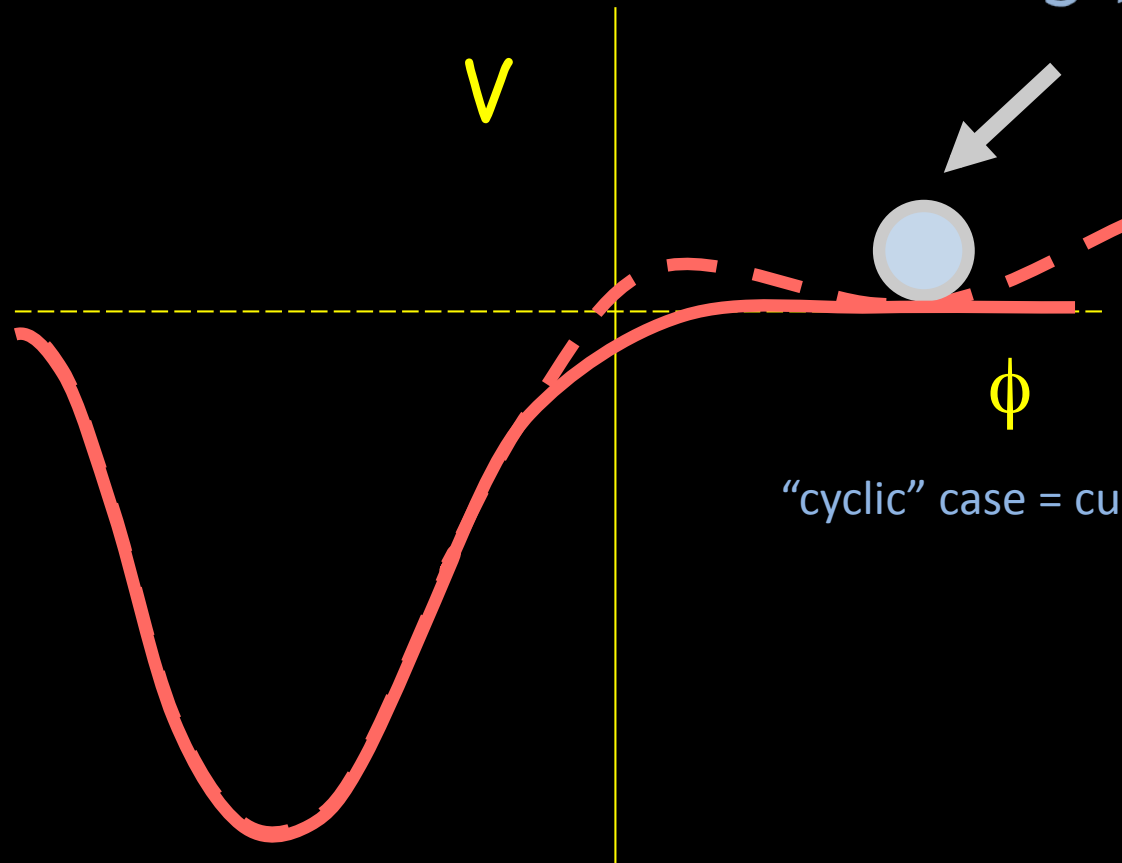


No eternal runaway !

$$w = \frac{\frac{1}{2}\dot{\phi}^2 - V(\phi)}{\frac{1}{2}\dot{\phi}^2 + V(\phi)}$$

entropically favorable initial condition

$$S > 10^{120}$$



“cyclic” case = current condition

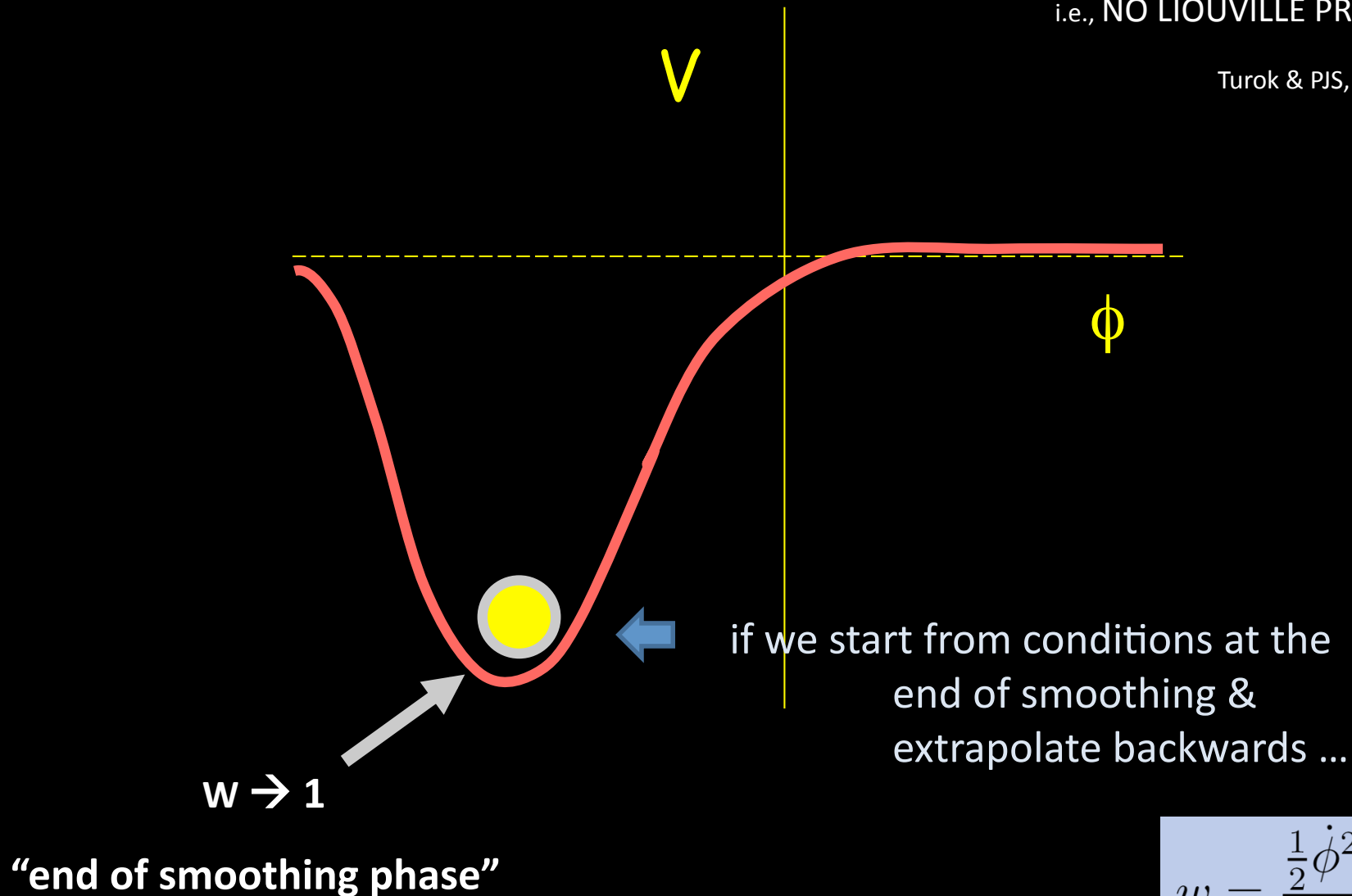
$$w = \frac{\frac{1}{2}\dot{\phi}^2 - V(\phi)}{\frac{1}{2}\dot{\phi}^2 + V(\phi)}$$

extrapolating backwards: $KE \sim 1/a^6$ shrinks as $a \rightarrow \text{increases}$

$|PE| \rightarrow \text{also decreases as } 1/a^6$

i.e., NO LIOUVILLE PROBLEM

Turok & PJS, to appear



$$w = \frac{\frac{1}{2}\dot{\phi}^2 - V(\phi)}{\frac{1}{2}\dot{\phi}^2 + V(\phi)}$$

In sum, with a bounce & no inflation:

Can causally smooth

Can flatten

Can isotropize

Can make density perturbations

Avoid eternal runaway

Avoid Liouville/entropy (initial conditions) problem

Avoid axion overproduction

Can the big bang be a bounce ?

Gasperini & Veneziano

Brandenberg & Wafa

Khoury, Ovrut, PJS, Turok

Tsujikawa, Brandenberger, Finelli

Khoury, Buchbinder & Ovrut

Tolley, Turok, PJS

Biswas, Mazumdar, and Siegel

Bojaward

Cai, Qiu, Piao, Li, Zhang

Penrose

Turok, Craps, Hertog

Cai, Brandenberger, Zhang

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.

big crunch/big bang transition

Itzhak Bars, Shih-Hung Chen, PJS and Neil Turok
arxiv:1112.2470

Introduces a Weyl invariant extension of Einstein gravity

For appropriate choice of Weyl gauge, find geodesically complete solutions with big crunch/big bang transition

Unique solution that preserves unitarity, analyticity, momentum

Wheeler-de Witt equation produces same results (to appear)

Analytic continuation in complex- t plane produces similar results (to appear)

What Next for Cosmology ?

Big Bang:
Beginning or Bounce ?

Unitarity, Emergence of Time, Null Energy Condition

big crunch/big bang transition

Itzhak Bars, Shih-Hung Chen, PJS and Neil Turok

After the smoothing phase , life is simple as we approach the bounce!

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{2\kappa^2} R(g) - \frac{1}{2} (\partial\sigma)^2 + \text{radiation} \right]$$

Smooth & Flat; Massless degrees of freedom; Ultralocal

Natural to consider a “Weyl invariant extension” :

$$S = \int d^4x \sqrt{-g} \left[\frac{(\partial\phi)^2 - (\partial s)^2}{2} + \frac{\phi^2 - s^2}{12} R + \text{radiation} \right]$$

Weyl invariant: $g_{\alpha\beta} \rightarrow e^{2\omega(x)} g_{\alpha\beta}$, $\phi \rightarrow e^{-\omega(x)} \phi$ and $s \rightarrow e^{-\omega(x)} s$

fix $\omega(x)$ so that $\frac{1}{12}(\phi^2 - s^2) = 1/2\kappa^2$ to recover Einstein eqs.

Every solution of the Einstein equations

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{2\kappa^2} R(g) - \frac{1}{2} (\partial\sigma)^2 + \text{radiation} \right]$$

... is also a solution of the Weyl invariant extension ...

$$S = \int d^4x \sqrt{-g} \left[\frac{(\partial\phi)^2 - (\partial s)^2}{2} + \frac{\phi^2 - s^2}{12} R + \text{radiation} \right]$$

... and also a solution of other gauge-fixed versions (e.g., $g = a = 1$)

$$S = \int d^4x \sqrt{-g} \left[\frac{(\partial\phi)^2 - (\partial s)^2}{2} + \frac{\phi^2 - s^2}{12} R + \text{radiation} \right]$$

➔
$$\int d\tau \left\{ \frac{1}{2e} \left[-\dot{\phi}^2 + \dot{s}^2 + \frac{\kappa^2}{6} (\phi^2 - s^2) (\dot{\alpha}_1^2 + \dot{\alpha}_2^2) \right] - e\rho_r \right\}$$

Can translate from one to the other:

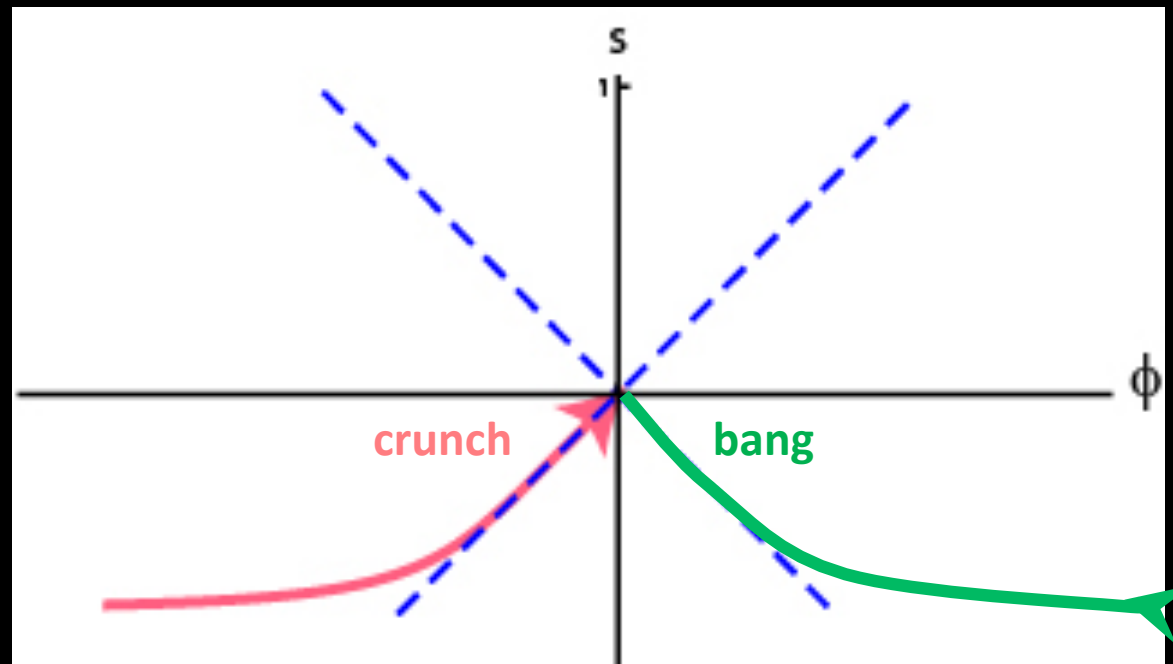
$$a_E^2 \equiv \frac{\kappa^2}{6} (\phi^2 - s^2)$$

BUT ... geodesically incomplete solutions in one
may be geodesically complete solutions in the other !

$$\int d\tau \left\{ \frac{1}{2e} \left[-\dot{\phi}^2 + \dot{s}^2 + \frac{\kappa^2}{6} (\phi^2 - s^2) (\dot{\alpha}_1^2 + \dot{\alpha}_2^2) \right] - e\rho_r \right\}$$

$$a_E^2 \equiv \frac{\kappa^2}{6} (\phi^2 - s^2)$$

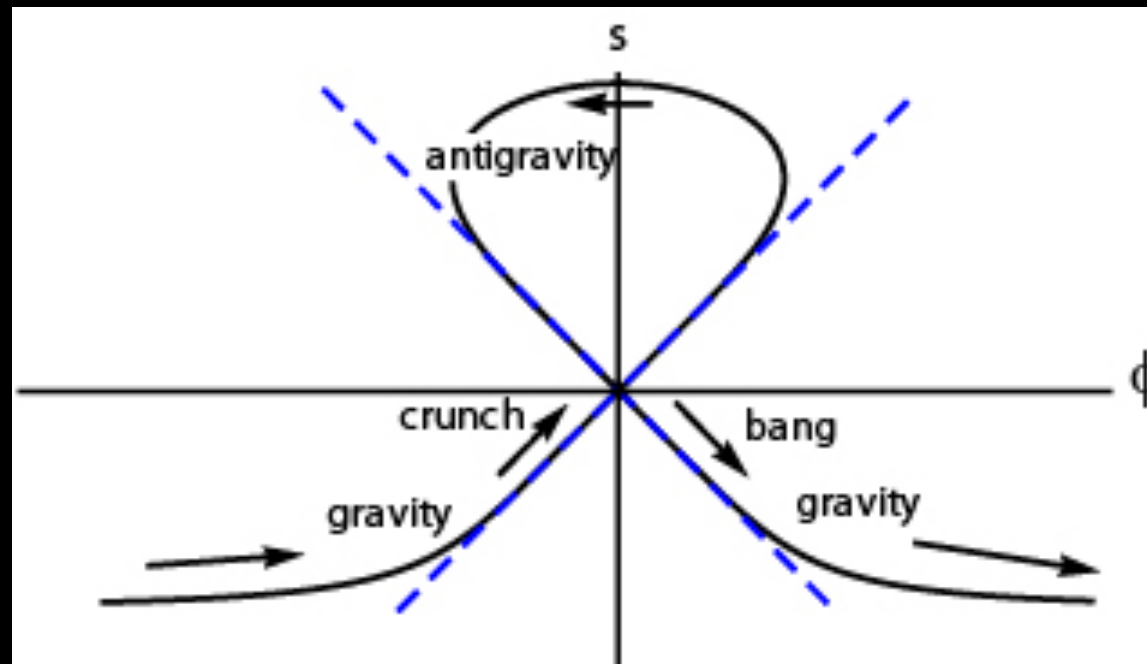
Einstein gauge: incomplete at $a_E = 0$



$$\int d\tau \left\{ \frac{1}{2e} \left[-\dot{\phi}^2 + \dot{s}^2 + \frac{\kappa^2}{6} (\phi^2 - s^2) (\dot{\alpha}_1^2 + \dot{\alpha}_2^2) \right] - e\rho_r \right\}$$

$$a_E^2 \equiv \frac{\kappa^2}{6} (\phi^2 - s^2)$$

New gauge: geodesically complete!

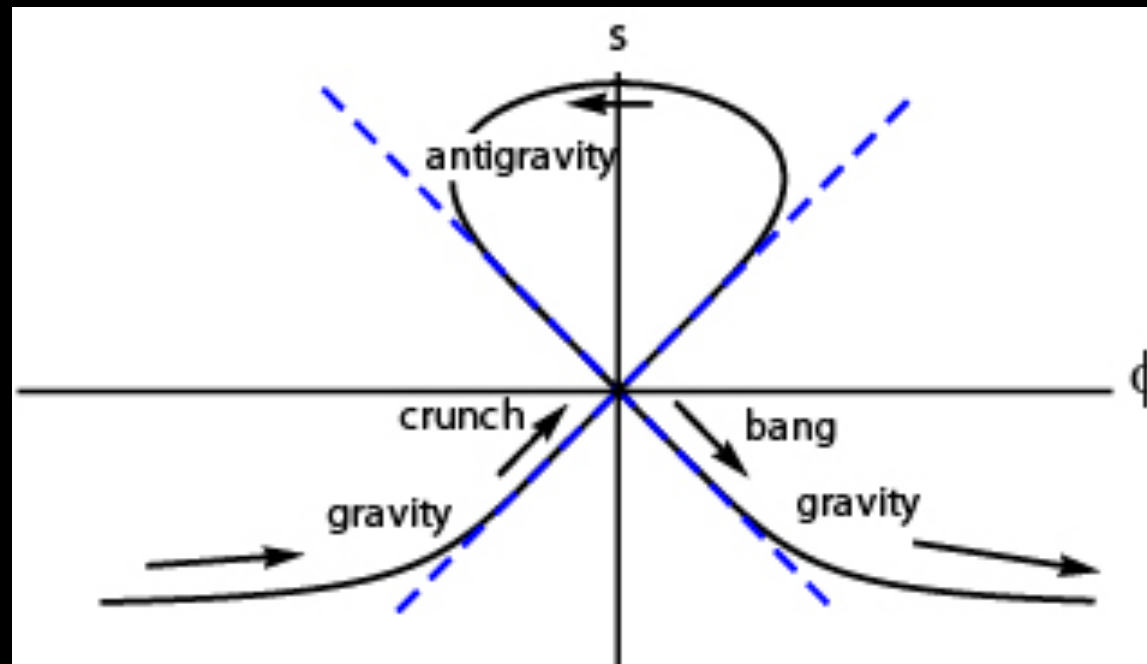


$$S = \int d^4x \sqrt{-g} \left[\frac{(\partial\phi)^2 - (\partial s)^2}{2} + \frac{\phi^2 - s^2}{12} R + \text{radiation} \right]$$

$$\int d\tau \left\{ \frac{1}{2e} \left[-\dot{\phi}^2 + \dot{s}^2 + \frac{\kappa^2}{6} (\phi^2 - s^2) (\dot{\alpha}_1^2 + \dot{\alpha}_2^2) \right] - e\rho_r \right\}$$

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New gauge: geodesically complete!



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